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INFRARED AND SUBMILLIMETER EXTINCTION BY FOG.(U)

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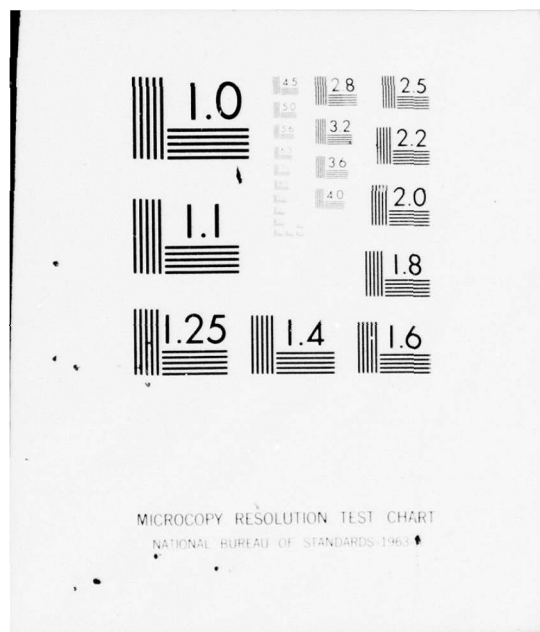
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TECHNICAL REPORT TR-77-9

INFRARED AND SUBMILLIMETER EXTINCTION
BY FOG

Physical Sciences Directorate
Technology Laboratory

14 July 1977



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| REPORT DOCUMENTATION PAGE | | READ INSTRUCTIONS BEFORE COMPLETING FORM |
|--|--|---|
| 1. REPORT NUMBER 14 DRDMI-TR-77-9 | 2. GOVT ACCESSION NO. | 3. RECIPIENT'S CATALOG NUMBER |
| 4. TITLE (and Subtitle) 6 INFRARED AND SUBMILLIMETER EXTINCTION BY FOG | 5. TYPE OF REPORT & PERIOD COVERED 9 Technical Report | |
| 7. AUTHOR(s) 10 Dorathy Anne Stewart | 6. PERFORMING ORG. REPORT NUMBER TR-77-9 | |
| 9. PERFORMING ORGANIZATION NAME AND ADDRESS Commander US Army Missile Research and Development Command Attn: DRDMI-TR Redstone Arsenal, Alabama 35809 | 8. CONTRACT OR GRANT NUMBER(s) | |
| 11. CONTROLLING OFFICE NAME AND ADDRESS Commander US Army Missile Research and Development Command Attn: DRDMI-TI Redstone Arsenal, Alabama 35809 | 10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS DA 11L161102AH49 17 00 AMCMS Code 611102, H490011 | |
| 12. REPORT DATE 14 July 1977 | 13. NUMBER OF PAGES 61 1349k | |
| 14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) | 15. SECURITY CLASS. (of this report) UNCLASSIFIED | |
| 15a. DECLASSIFICATION/DOWNGRADING SCHEDULE | | |
| 16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited. | | |
| 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report) | | |
| 18. SUPPLEMENTARY NOTES | | |
| 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Fog drop sizes Propagation Visibility Infrared Submillimeter | | |
| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A thorough literature survey of fog drop-size distributions throughout the world is discussed, and data from 36 references are summarized. The review of an extensive list of over 100 references includes additional important information. Ranges of liquid water content and problems of relating this to ABSTRACT (Continued) | | |

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ABSTRACT (Concluded)

visibility are examined. Changes in fog characteristics from place to place and from time to time are also considered, and the discussion includes small-scale spatial and temporal fluctuations. ↑

A representative sample of data is used to compute extinction of electromagnetic energy with wavelengths of 0.55, 10.5, 870, and 1250 μm . Extinction of the 1250- μm wavelength by fog droplets is always less than extinction of the 870- μm wavelength. Extinction of the 870- μm energy by fog droplets is always less than extinction of the visible and the 10.5- μm energy. The relationship between the visible and the infrared extinction depends upon the drop-size distribution. The 10.5- μm wavelength is frequently attenuated about the same amount as the visible, and it is not uncommon for the infrared extinction to be greater than the visible extinction.

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ACKNOWLEDGMENTS

The author would like to express her appreciation to Dr. Oskar M. Essenwanger for encouragement and helpful suggestions during this project. She would also like to thank Dr. Bobby D. Guenther for calling her attention to an important publication. Personnel at Redstone Scientific Information Center deserve credit for their extra efforts to obtain some obscure publications. Finally, thanks are due to Mrs. Clara B. Brooks for her care in typing the manuscript.

I. INTRODUCTION

Fog, mist, and haze are obstructions to visibility. Fog exists when the atmosphere contains a suspended aggregate of very small water drops which reduce the horizontal visibility to 1 km or less near the surface. When an aggregate of water droplets suspended in the atmosphere near the surface does not reduce visibility as low as 1 km, it is called mist. Mist is intermediate between fog and haze. Haze consists of particles which are so small they cannot be felt or individually seen with the eye. Haze particles may be dry or damp. More detailed definitions may be found in the Glossary of Meteorology (Huschke, 1959). Eldridge (1969) discusses alternate definitions which exist in the literature.

This report is primarily concerned with fog, but first, a few references will be listed for the reader who is interested in visibilities greater than 1 km. Wells et al. (1977), Hänel (1971), Mészáros (1971), and Laktionov (1967a) contain information about the size of particles and visibility as a function of relative humidity. Johnson (1976) shows that ultragiant aerosols with radii of 15 μm and larger are not rare. Flanigan and DeLong (1970) and Hoidale and Blanco (1969) discuss measurements of infrared characteristics of dust. Gordin and Strelkov (1975) and Carlon (1970) consider infrared characteristics of very fine water aerosol.

Fog is formed by a variety of meteorological processes.

When the ground loses heat at night by radiational cooling through a clear atmosphere, radiation fog will form if the air cools enough to become supersaturated.

Advection fog is fog which forms when warm, moist air moves across water or land which has a lower temperature.

Frontal fog is associated with a frontal passage. Frontal fog may be caused by rain falling into cooler air or by mixing of different air masses near the frontal zone. Some authors call the former an evaporation fog and the latter a mixing fog.

An upslope fog is formed when air flows upward over rising terrain and cools adiabatically to the dew point.

Steam fog, which is also called evaporation fog, is formed when cold air moves over a warmer body of water or when warm rain falls through a layer of colder air.

Further information of a general nature may be found in standard references such as Berry et al. (1945), Huschke (1959), Landsberg (1958), and Schönwiese (1970).

Mathematical and numerical models describing different characteristics of fog are found in Baronti and Elzweig (1973), Lala et al. (1975), Low (1975b), Magono et al. (1974), Rodhe (1962, 1966), and Weinstein (1974a, b).

II. COMPUTATIONAL PROCEDURE

When electromagnetic energy propagates through an atmosphere which contains scattering and absorbing particles, the extinction coefficient σ , which is also called the attenuation coefficient, is given by the following formula:

$$\sigma = \sum_i \pi r_i^2 (Q_{\text{ext}})_i N_i \quad ,$$

where r_i is the radius of particles in the i th interval which contains N_i particles per cubic unit of length. To be precise, the r_i^2 which is used in the computation should be the mean square radius over the interval. $(Q_{\text{ext}})_i$ is the mean extinction efficiency factor (also called the relative extinction coefficient or the normalized extinction cross section) in the i th radius interval. Q_{ext} is a dimensionless function of drop size, wavelength of electromagnetic energy, and the complex index of refraction. The extinction coefficient σ is in units of inverse length. If σ is in units of m^{-1} , the attenuation in decibels/kilometer may be obtained by multiplying by 4343.

Johnson (1954) has shown that if one assumes a threshold of brightness contrast of 0.02, one may compute the visibility V according to the formula

$$V = \frac{3.912}{\sigma} ,$$

where σ is computed for some wavelength near the middle of the visible range.

If the units of σ are m^{-1} , the visibility is in meters.

Mie (1908) developed a theory to describe scattering and absorption of electromagnetic energy by spherical particles with a known complex index of refraction $m = n - ik$. Modern discussions and explanations of electromagnetic propagation theory can be found in Kerker (1969), McCartney (1976), Deirmendjian et al. (1961), Weeks (1964), Stephens et al. (1971), and Verner (1976). A summary of the procedure used in this report follows.

The extinction efficiency factor is related to the complex numbers a_n and b_n by the formula

$$Q_{\text{ext}} = \frac{2}{\alpha} \sum_{n=1}^{\infty} (2n+1) [\text{Re}(a_n + b_n)] .$$

The dimensionless parameter α is the ratio of the circumference of the drop to the wavelength of radiant energy and is defined by

$$\alpha = \frac{2\pi r}{\lambda} .$$

The wavelength λ must be expressed in the same units as the radius.

The quantities a_n and b_n are defined by

$$a_n = \frac{\psi_n(\alpha) \psi_n'(\beta) - m \psi_n(\beta) \psi_n'(\alpha)}{\xi_n(\alpha) \psi_n'(\beta) - m \psi_n(\beta) \xi_n'(\alpha)}$$

and

$$b_n = \frac{m\psi_n(\alpha)\psi'_n(\beta) - \psi_n(\beta)\psi'_n(\alpha)}{m\zeta_n(\alpha)\psi'_n(\beta) - \psi_n(\beta)\zeta'_n(\alpha)},$$

where $\beta = m\alpha$ and $\zeta = \psi + i\chi$. The prime denotes differentiation with respect to the argument. The quantities ψ and χ are Ricatti-Bessel functions defined as

$$\psi_n(x) = \left(\frac{\pi x}{2}\right)^{1/2} J_{n+1/2}(x)$$

and

$$\chi_n(x) = -\left(\frac{\pi x}{2}\right)^{1/2} N_{n+1/2}(x),$$

where $J_{n+1/2}(x)$ and $N_{n+1/2}(x)$ are half integral order Bessel and Neumann functions of any argument x .

For computational purposes, one may define the appropriate quantities for $n = 0$ and $n = 1$ and use an iterative procedure to obtain higher order terms

$$\psi_0(x) = \sin x$$

$$\psi_1(x) = \frac{\sin x}{x} - \cos x$$

$$\chi_0(x) = \cos x$$

$$\chi_1(x) = \frac{\cos x}{x} + \sin x.$$

When x is a complex number such as β , the preceding functions transform into functions of hyperbolic sines and cosines according standard equations.

The equations for finding higher order terms of ψ and χ are

$$Z_{n+1}(x) = \frac{2n+1}{x} Z_n(x) - Z_{n-1}(x)$$

and

$$\begin{aligned} Z'_n(x) &= \frac{n+1}{x} Z_n(x) - Z_{n+1}(x) \\ &= \frac{1}{2n+1} \left[(n+1)Z_{n-1}(x) - nZ_{n+1}(x) \right], \end{aligned}$$

where Z is either ψ or χ and x is α or β .

The accuracy of the computer programs has been checked by making test calculations for comparison with tables published by the US Bureau of Standards (1949), Gumprecht and Sliepcevich (1951), Penndorf (1957), Irvine and Pollack (1968), and Appendix J of McCartney (1976). Gumprecht and Sliepcevich, Penndorf, and McCartney only deal with real indices of refraction. Irvine and Pollack's tables are quite extensive. They cover many wavelengths and a few drop radii for complex indices of refraction of water and ice. The publication by the US Bureau of Standards is particularly useful for checking computations because it includes values of a_n and b_n and it considers real and complex indices of refraction.

One might also note that Chýlek (1975, 1977) has shown that the extinction efficiency factor approaches a limiting value of two as α becomes infinite for all values of the index of refraction, but the limiting value of the scattering efficiency factor is a function of the refractive index.

Mie theory is quite reliable for spherical scatterers. For example, Dobbins and Eklund (1977) have recently shown that the smallest scale of fluctuations predicted by the theory can be measured in the laboratory.

Fog water droplets are nearly spherical, but ice particles are not spherical. Any reader interested in nonspherical particles is advised to consult Zerull et al. (1977).

Table 1 contains the indices of refraction which were used to make the computations discussed in Section IV of this report. These computations are not highly sensitive to small changes in the index of refraction, and the results would have been qualitatively the same if sources other than Davies et al. (1970) and Hale and Querry (1973) had been used.

A few other sources of data will be noted for the interested reader. Deirmendjian (1975), Downing and Williams (1975), Rozenberg (1974), Irvine and Pollack (1968), and Kislovskii (1959) contain indices of refraction for several wavelengths. Additional information about indices of refraction of water near 1 mm can be found in Chamberlain et al. (1973), Apletalin et al. (1970), and Goronina et al. (1966). The preceding references are concerned with pure water or ice, but Querry et al. (1977) have studied relative reflectance and complex refractive index in the infrared for various samples of saline environmental waters.

Figure 1 is a conventional graph of Q_{ext} versus α for wavelengths of 0.55 and 10.5 μm . This graph has been slightly smoothed because the smaller scale ripple structure is not important for our purposes.

TABLE 1. INDICES OF REFRACTION

| Source | Wavelength (μm) | Index of Refraction |
|------------------------|---------------------------------|----------------------------|
| Hale and Querry (1973) | 0.55 | $1.333 - 1.96 (10^{-9}) i$ |
| Hale and Querry (1973) | 10.5 | $1.185 - 0.0662 i$ |
| Davies et al. (1970)* | 870 | $2.422 - 0.9667 i$ |
| Davies et al. (1970) | 1250 | $2.630 - 1.1407 i$ |

*The index of refraction for 870 μm is an interpolated value.

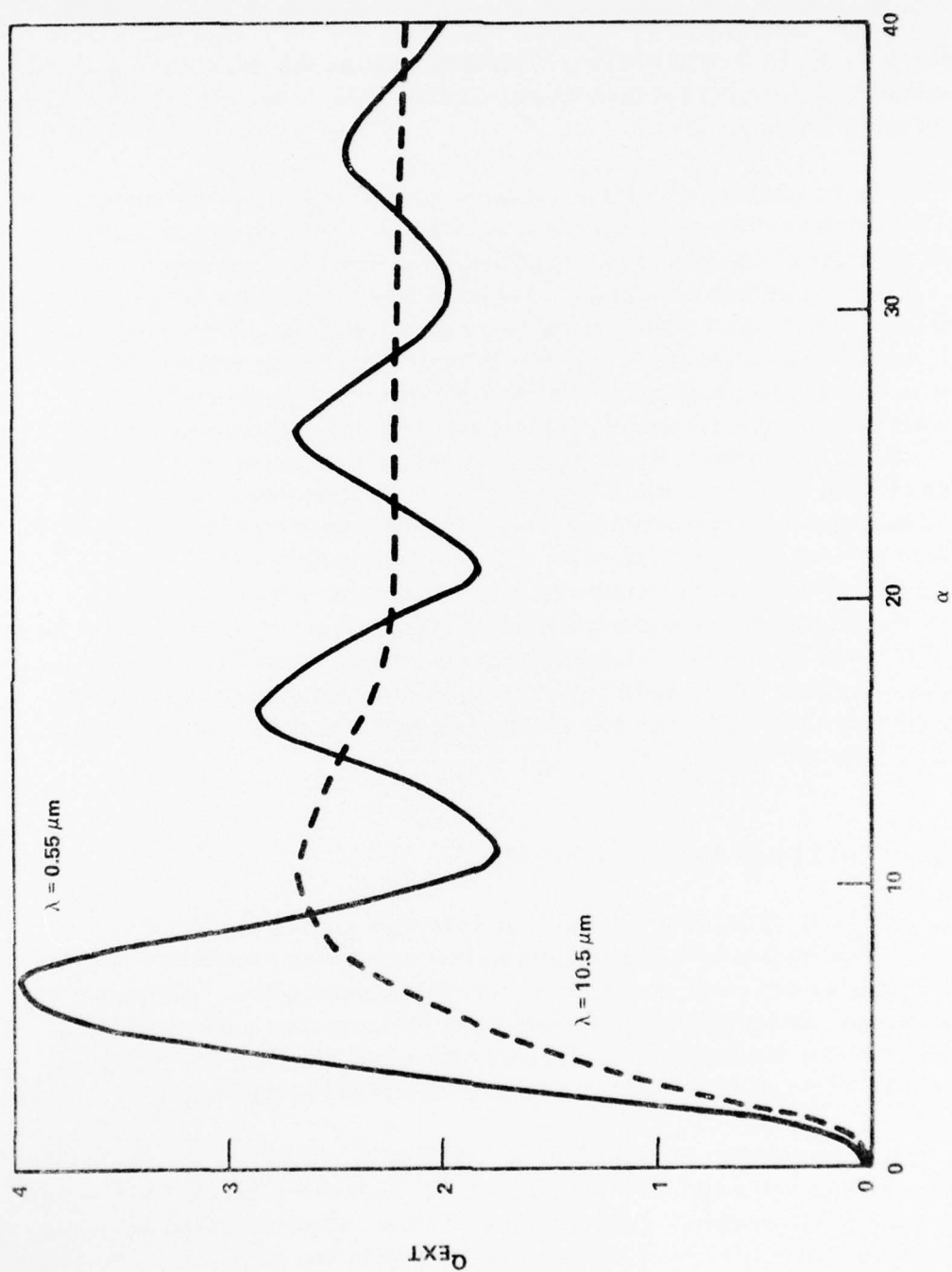


Figure 1. Q_{ext} versus α for 0.55 and 10.5 μm .

In Figure 2, Q_{ext} is graphed as a function of droplet radius for wavelengths of 0.55, 10.5, and 870 μm . This graph shows that extinction is actually greater for 10.5- μm energy than for the visible energy when particles are larger than about 10 μm in radius.

Table 2 contains a sample computation of extinction for a hypothetical fog drop-size distribution. The purpose of showing this computation is to demonstrate the relative importance of small and large drops to atmospheric extinction. It has sometimes been argued that many measurement techniques discriminate against small drops, and this computation should demonstrate the small importance of this fact. The hypothetical distribution differs from one of the measured distributions only in the first three radius intervals. No particles in the corresponding real distribution were recorded with radii less than 1 μm . There were 5.5 particles per cubic centimeter in the 1- to 2- μm radius interval and 4.8 particles per cubic centimeter in the 2- to 3- μm interval. Thus, the computed visibility for the hypothetical distribution in Table 2 is 221 m as compared with 248 m for the measured distribution. However, if the 0.9 particles per cubic centimeter with radii greater than 15 μm were removed from Table 2, and everything else remained the same, the computed visibility would be 245 m. Therefore, one sees that eliminating 170 particles per cubic centimeter with radii less than 3 μm for the distribution in Table 2 has almost the same effect as eliminating 0.9 particles per cubic centimeter with radii greater than 15 μm .

III. FOG DROP-SIZE DISTRIBUTIONS

Radii of fog drops range from less than 1 μm to slightly over 100 μm . This section will include information concerning variations from one place to another and from one fog to another in the same place. Although some variations are caused by biases in methods of measurement as suggested by Eldridge (1971), instrumental limitations cannot explain all of the variations in Table 3, which summarizes the data to be discussed in this section.

The very thorough investigation by Arnulf et al. (1957) in France is often quoted. The experimental work was done at St. Inglevert (Pas-de-Calais) near the sea and at Villacoublay, an airport near Paris. They measured drop-size distributions and extinction of several wavelengths in hazes and fogs. No radii greater than 15 μm were shown on their graphs, and the main mode was near 2.5 μm for all data. Large secondary modes did not appear. In hazes, the

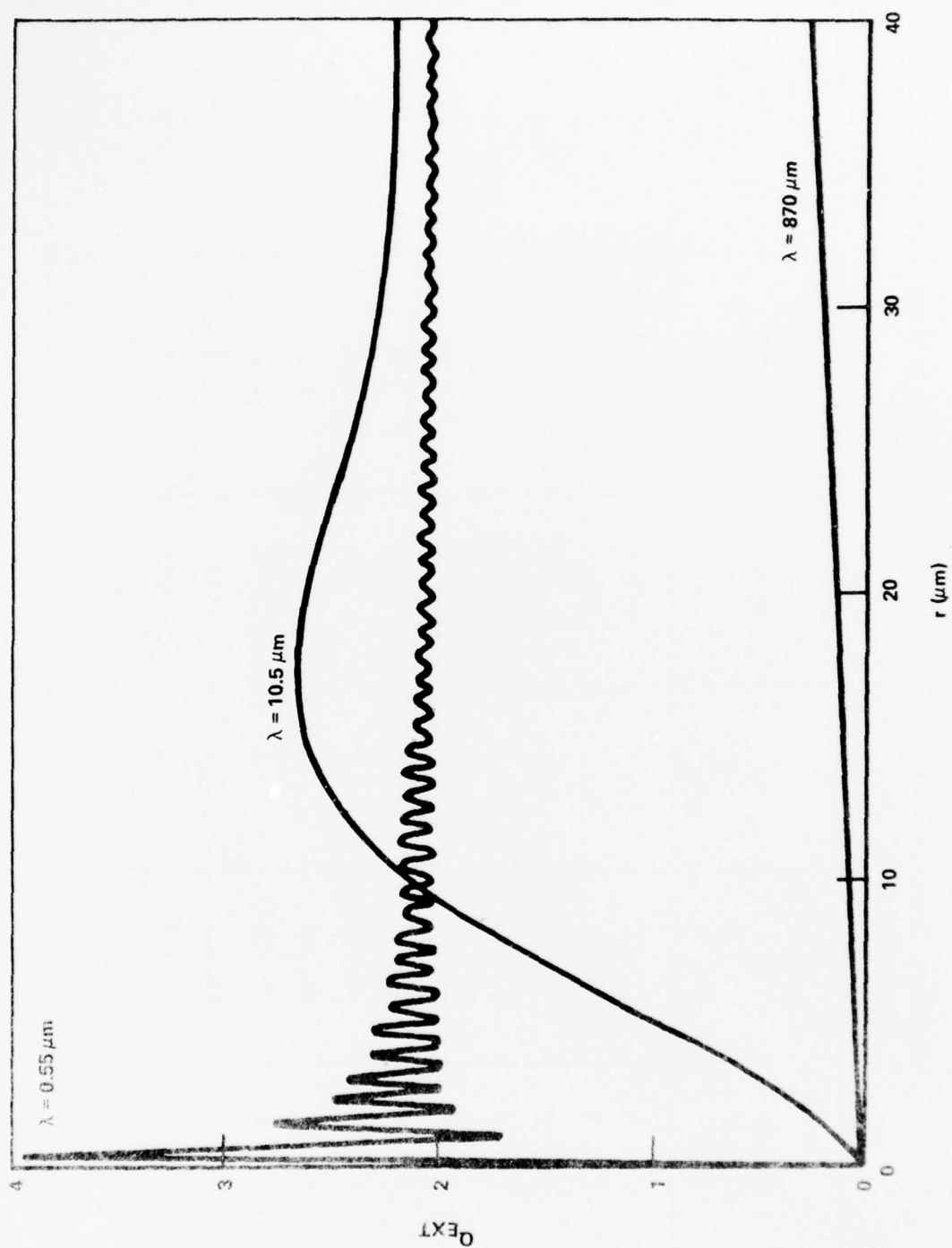


Figure 2. Q_{ext} versus r for 0.55, 10.5, and 870 μm .

TABLE 2. SAMPLE OF COMPUTATIONAL PROCEDURE FOR OBTAINING
EXTINCTION COEFFICIENT

| Radius Interval (μm) | $\overline{r_i^2}$ (μm^2) | N_i (cm^{-3}) | $\overline{\pi r_i^2 N_i}$ (km^{-1}) | $\overline{\pi r_i^2 N_i Q_i}$ for $0.55 \mu\text{m}$ (km^{-1}) | $\overline{\pi r_i^2 N_i Q_i}$ for $10.5 \mu\text{m}$ (km^{-1}) |
|---|---|-------------------------------|--|--|--|
| 0 to 1 | 0.333 | 100.0 | 0.1047 | 0.23 | 0.01 |
| 1 to 2 | 2.333 | 55.5 | 0.4068 | 0.91 | 0.07 |
| 2 to 3 | 6.333 | 24.8 | 0.4934 | 1.11 | 0.18 |
| 3 to 4 | 12.333 | 3.1 | 0.1201 | 0.27 | 0.07 |
| 4 to 5 | 20.333 | 4.7 | 0.3002 | 0.65 | 0.25 |
| 5 to 6 | 30.333 | 4.4 | 0.4193 | 0.88 | 0.46 |
| 6 to 7 | 42.333 | 4.0 | 0.5320 | 1.12 | 0.72 |
| 7 to 8 | 56.333 | 7.6 | 1.3450 | 2.84 | 2.12 |
| 8 to 9 | 72.333 | 4.2 | 0.9544 | 2.01 | 1.72 |
| 9 to 10 | 90.333 | 3.0 | 0.8514 | 1.78 | 1.70 |
| 10 to 11 | 110.333 | 2.4 | 0.8319 | 1.72 | 1.80 |
| 11 to 12 | 132.333 | 1.1 | 0.4573 | 0.95 | 1.06 |
| 12 to 13 | 156.333 | 0.5 | 0.2456 | 0.51 | 0.60 |

TABLE 2. (Concluded)

| Radius Interval (μm) | $\overline{r_i^2}$ (μm^2) | N_i (cm^{-3}) | $\overline{\pi r_i N_i}$ (km^{-1}) | $\overline{\pi r_i N_i G_i}$ for $0.55 \mu\text{m}^*$ (km^{-1}) | $\overline{\pi r_i N_i Q_i}$ for $10.5 \mu\text{m}^*$ (km^{-1}) |
|---|---|-------------------------------|--|--|--|
| 13 to 14 | 182.333 | 0.5 | 0.2864 | 0.59 | 0.72 |
| 14 to 15 | 210.333 | 0.3 | 0.1982 | 0.41 | 0.51 |
| 15 to 16 | 240.333 | 0.3 | 0.2265 | 0.47 | 0.60 |
| 16 to 17 | 272.333 | 0.3 | 0.2567 | 0.53 | 0.68 |
| 17 to 18 | 306.333 | 0.0 | 0.0000 | 0.00 | 0.00 |
| 18 to 19 | 342.333 | 0.0 | 0.0000 | 0.00 | 0.00 |
| 19 to 20 | 380.333 | 0.3 | 0.3585 | 0.73 | 0.94 |

* $\sigma(0.55) = 17.71 \text{ km}^{-1}$ and $\sigma(10.5) = 14.21 \text{ km}^{-1}$.

TABLE 3. SUMMARY OF MEASUREMENTS OF FOG DROPLET RADII

| Source | Typical Radii (μm) | Maximum Radius (μm) | Miscellaneous Information |
|---------------------------|------------------------------------|-------------------------------------|-------------------------------------|
| Arnulf et al. (1957) | 2.5 | 15 | France |
| Best (1951) | 5 to 12 | 40 | From earlier work by Hagemann |
| Cong and Dessens (1973) | 8 to 10 | 22 | Localized near plume from pulp mill |
| Deloncle (1963) | 4.5 to 5.2 | 17 | Widespread through valley |
| | <1 | 10 | Urban, near Paris |
| | <0.75 | 8 | Mountain top, France |
| Dickson et al. (1975) | 3.4 | 118 | Capistrano, California |
| Donaldson (1955) | 10 to 25 | 100 | Massachusetts |
| Eldridge (1961) | <1 | 32 | Massachusetts |
| Findeisen (1932) | 1 to 4 | 60 | Hamburg, Germany |
| Garland (1971) | <1 | 40 | Radiation fogs, all water |
| | 10 | 70 | Radiation fogs, ice crystals |
| | 4 | 60 | Advection fogs |
| Garland et al. (1973) | <0.6 | 20 | Radiation fogs |
| Gathman and Larson (1974) | 3 to 9 | 64 | Greenland Sea |
| Gorchakov (1972) | 5.5 to 12.5 | | Russia |

TABLE 3. (Continued)

| Source | Typical Radii (μm) | Maximum Radius (μm) | Miscellaneous Information |
|--------------------------------|------------------------------------|-------------------------------------|---|
| Grunow (1960) | 1.5 4 to 7 6 to 9 | 7.5 12.5 30 | Mt. Hohenpeissenberg, Germany Polar air Maritime air Continental air |
| Houghton and Radford (1938) | 4 to 35 | 65 | Typically advection fogs |
| Jiusto (1964) | 5 10 | 17.5 32.5 | Radiation Advection |
| Kozima et al. (1953) | 2.5 to 7.5 | 55 | Japan |
| Kumai (1973) | 3.5 to 12.6 | 65 | Point Barrow, Alaska; advection fogs |
| Kunkel (1971) | 5 to 10 | 45 | Otis Air Force Base |
| Low (1975) | 9 to 13 4 to 13 | 21 | Radiation fog, Ft. Rucker, Alabama Mixed radiation-advection, California |
| Ludwig et al. (1974) | 0.1 | 15 | Radiation fog |
| Mack et al. (1973) | 4 to 8 | 31 | At sea |

TABLE 3. . (Continued)

| Source | Typical Radii (μm) | Maximum Radius (μm) | Miscellaneous Information |
|-------------------------------|------------------------------------|-------------------------------------|---|
| May (1961) | <0.5 to 15 | 160 | Salisbury Plain, England |
| Mészáros (1965) | <0.4 to 10 2 to 13 | 43.8 101.5 | Budapest, Hungary Radiation Advection |
| Okita (1962) | 6 to 17 | 60 | Radiation fogs in Japan |
| Pedersen and Tødsen (1960) | <2 2 | 16 25 | Oslo, Norway Radiation Advection |
| Pillé et al. (1975) | 3 to 12 | 31 | Chemung River Valley, New York |
| Reinking (1975) | 3 | 7.5 | San Joaquin Valley, California |
| Roberts (1976) | 0.2 to 1.1 | 8 | Grafenwöhr, Germany |
| Rogers et al. (1974) | 8 | 115 | California coast |
| Rozenberg (1974) | 5 50 | | Thin Medium |
| Tag (1976) | 8 | 23 | Panama Canal Zone |

TABLE 3. (Concluded)

| Source | Typical Radii (μm) | Maximum Radius (μm) | Miscellaneous Information |
|-------------------------------|------------------------------------|-------------------------------------|--|
| Tampieri and Tomasi (1976) | 8 | 22 | Radiation fog, Italy |
| Thompson et al. (1967) | 10 | 34 | Otis Air Force Base |
| Thuman and Robinson (1953) | 40 32 15 | | Ice prisms Ice hexagons Ice droxtals |
| Tverskoi (1965) | 1.5 2 | 60 60 | Radiation fog Evaporation fog |
| Webb (1956) | 5 to 19 | 70 | Washington, D. C. and Virginia |

optical densities were 10 to 15 times larger in the visible than at $10\ \mu\text{m}$. In fogs which they called selective fogs atmospheric extinction of visible wavelengths varied from about 2 to over 20 times the extinction at a wavelength of $10\ \mu\text{m}$. In evolving fogs, visible wavelengths were attenuated from about 1.4 to 20 times the wavelength of $10\ \mu\text{m}$. In stable fogs the $10\text{-}\mu\text{m}$ attenuation was always at least half the visible attenuation, and in some stable fogs attenuation at $10\ \mu\text{m}$ was almost as much as in the visible.

Best (1951) discussed a paper published by Hagemann (1936) from Hamburg, Germany, but Best's paper is probably more readily available. The peaks of the drop-size distributions illustrated in Hagemann's Figure 6 were typically from about 5- to $12\text{-}\mu\text{m}$ radius. Maximum drop sizes measured by Hagemann were near $40\ \mu\text{m}$, and most samples contained a considerable number of drops with radii greater than $10\ \mu\text{m}$. The samples in Hagemann's original articles showed that many distributions were multimodal, and this was unfortunately lost in Best's parameterization.

Bimodal and multimodal distributions have also been inadequately parameterized by most other investigators. Essenwanger (1976) pointed this out in his discussion of Mallow (1975). Rensch and Long (1970), Baronti and Elzweig (1973), and Tampieri and Tomasi (1976a, b) also used distribution functions which allowed only a single mode.

Cong and Dessens (1973) made measurements in France on the upper Garonne River near a pulp mill which ejected 65 tons of water vapor per hour into the atmosphere. Measurements were made in a valley where wind speeds were light or it was calm, and there were frequent inversions. They studied two fogs which were spread throughout the valley basin and two fogs which were localized in the vicinity of the falling from the plume emitted by the pulp mill. Drops were larger in the localized fogs which had mean radii of 8 and $10\ \mu\text{m}$. Maximum radii were about $22\ \mu\text{m}$. Mean radii in the more widespread fogs were 4.5 and $5.2\ \mu\text{m}$, and maximum radii were about $17\ \mu\text{m}$. In both cases, large numbers of drops had radii greater than $10\ \mu\text{m}$.

Deloncle (1963a, b) studied fogs near Paris and on a mountain, Puy-de-Dôme, in France. Near Paris, most drops had radii less than $1\ \mu\text{m}$; the maximum radius was about $10\ \mu\text{m}$. Some of these distributions were bimodal (see Figure 5 of Deloncle, 1963a) with a secondary maximum near $5.5\ \mu\text{m}$. Deloncle found smaller drops on the mountain Puy-de-Dôme. Maximum radii were about $8\ \mu\text{m}$, and the largest number of drops had radii less than $0.75\ \mu\text{m}$. Even the secondary modal radius was only about $1.5\ \mu\text{m}$.

Dickson et al. (1975) made extensive measurements at Capistrano Test Site in California. Most of the data were in the form of computer printouts, but a typical example of fog was discussed in Volume I. The maximum radius of drops measured in this example was $118\text{ }\mu\text{m}$, but most drops had radii less than $82\text{ }\mu\text{m}$. The main modal radius was about $3.4\text{ }\mu\text{m}$, and there were very small secondary modes at 9.4 , 12.6 , and $19.4\text{ }\mu\text{m}$. Other fluctuations appeared to be too small to consider significant. The liquid water content was about 0.17 g/m^3 .

Donaldson (1955) made measurements near Buzzard's Bay in Massachusetts. According to Donaldson's Figure 6, volume mean radii in his samples varied from 16 to about $35\text{ }\mu\text{m}$. Therefore, the linear mean radii probably varied from about 10 to $25\text{ }\mu\text{m}$. From Donaldson's Figure 2, one sees that no large secondary modes were apparent, and the maximum drop-size was about 2.8 times the volume mean. It follows that the maximum drop-size must have been near $100\text{-}\mu\text{m}$ radius. Liquid water contents varied from about 0.013 to 0.16 g/m^3 .

Eldridge (1961) found that in 11 of 14 samples the number of drops increased monotonically as the droplet radius decreased. The smallest drop-size class in Eldridge's Tables 2 and 3 was 0.5- to $1\text{-}\mu\text{m}$ radius. The largest class was for radii from 16 to $32\text{ }\mu\text{m}$. In 2 of the 14 samples, the mode was in the 1- to $2\text{-}\mu\text{m}$ class; one sample had the mode in the 2- to $4\text{-}\mu\text{m}$ class. The liquid water content varied from 0.039 to 0.365 g/m^3 .

Findeisen (1932) measured drop-size distribution in fogs in Hamburg, Germany. All the samples illustrated in Findeisen's Figures 6 and 7 had large numbers of small drops and were multimodal. There were large numbers of drops with radii greater than $10\text{ }\mu\text{m}$. The five distributions in Findeisen's Figure 7 had at least one small secondary maximum with these larger radii. The maximum radius was about $60\text{ }\mu\text{m}$.

Garland (1971) had 25 sets of measurements in a table. The fogs were classified according to whether they were judged to be radiation fogs or advection fogs. Most calculated visual ranges were a little more than observed visual ranges and, perhaps, some small drops were missed. In radiation fogs with no ice crystals, droplet radii varied from 0.3 to $40\text{ }\mu\text{m}$. In a radiation fog which consisted entirely of ice, the radii varied from 6 to $70\text{ }\mu\text{m}$. In advection fogs the radii varied from 0.4 to $60\text{ }\mu\text{m}$. Garland's table did not give a typical or average radius, but I have estimated values from the information which was

given and from the graphs. Most drops apparently had radii less than $1\text{ }\mu\text{m}$ in the liquid radiation fogs. Ice fogs had typical radii greater than $6\text{ }\mu\text{m}$, probably at least $10\text{ }\mu\text{m}$. Advection fogs on the graphs in Figure 3 had typical radii from 2 to $8\text{ }\mu\text{m}$. Liquid water was in the range of 0.023 to 0.173 g/m^3 .

Garland et al. (1973) studied only radiation fogs. In five out of six samples the largest drops had radii of about $15\text{ }\mu\text{m}$; one sample had a drop with a radius as large as $20\text{ }\mu\text{m}$. In five out of six samples the category containing the most drops was less than $0.6\text{ }\mu\text{m}$. Large secondary modes did not occur. The liquid water content varied from 0.05 to 0.21 g/m^3 .

Gathman and Larson (1974) observed many atmospheric variables in three fogs in the Greenland Sea. They believed that their method of measurement was 100% efficient in collecting particles with radii greater than $1.0\text{ }\mu\text{m}$. Median radii in their 15 fog samples varied from 3 to $9\text{ }\mu\text{m}$ according to their Table 2. Their graphs were hard to read, but maximum drop radii apparently varied from about 32 to $64\text{ }\mu\text{m}$ in their Figures 8, 9, and 10. Calculated liquid water contents were in the range of 0.041 to 0.251 g/m^3 .

Gorchakov et al. (1972) made assumptions about the fog drop-size distributions and used an optical scattering technique to estimate the parameters in the distribution function for three cases. In two cases the modal radius was about $5.5\text{ }\mu\text{m}$. They were surprised that in the third case the mode was near $12.5\text{ }\mu\text{m}$, and the particle size distribution was quite narrow compared to the other two cases.

Grunow (1960) investigated fogs on Mt. Hohenpeissenberg in upper Bavaria in Germany. He found that cold polar air was characterized by droplets from 1- to $7.5\text{-}\mu\text{m}$ radius. Warm maritime air masses normally had droplets with radii from 2 to $12.5\text{ }\mu\text{m}$. Maritime air masses with a long continental trajectory had droplets from 2.5 to $30\text{ }\mu\text{m}$. Typical droplets in these three kinds of air masses had radii of 1.5, 4 to 7, and 6 to $9\text{ }\mu\text{m}$, respectively.

Houghton and Radford (1938) studied advection fogs at Round Hill in South Dartmouth, Massachusetts. They obtained 40 volume distribution curves in 16 fogs having peaks from 6- to $45\text{-}\mu\text{m}$ radius. The range of radii was from 1 to $65\text{ }\mu\text{m}$. Because the linear mean of radii is less than the radius of a droplet of mean volume, typical radii were probably from about 5 to $35\text{ }\mu\text{m}$. The largest liquid water content was about 0.3 g/m^3 .

Jiusto (1964) summarized a literature survey and divided fogs into two main types: radiation and advection. He assumed that inland fogs were radiation fogs and that coastal fogs were of the advection type. The average radius of radiation fog droplets was $5\text{ }\mu\text{m}$, and the maximum was about $17.5\text{ }\mu\text{m}$. The liquid water content was about 0.11 g/m^3 . The larger advection fog droplets had an average radius of about $10\text{ }\mu\text{m}$ and a maximum near $32.5\text{ }\mu\text{m}$. The liquid water content of advection fog was assumed to have an average of about 0.17 g/m^3 . Jiusto (1974), in a later article, has pointed out that these simplified numbers represent only typical values that will vary considerably in individual cases and with local conditions.

Kozima et al. (1953) divided the fog drop-size distributions that they measured in Hokkaido, Japan into four groups. Fogs containing particles with radii greater than $30\text{ }\mu\text{m}$ were type D. Type D typically had the largest number of particles in the smallest size category, and the number of particles decreased monotonically with increasing size. In type A fogs, 70% of the particles had radii less than $5\text{ }\mu\text{m}$. In type B fogs, less than 70% of the drops had radii less than $5\text{ }\mu\text{m}$ and less than 35% had radii greater than $10\text{ }\mu\text{m}$. More than 35% of the drops had radii greater than $10\text{ }\mu\text{m}$ in type C fogs, but none had radii greater than $30\text{ }\mu\text{m}$. The largest radii measured by Kozima et al. were $55\text{ }\mu\text{m}$.

Kumai's (1973) investigation of advection fogs in Point Barrow, Alaska, found maximum radii of $65\text{ }\mu\text{m}$. The categories with most drops varied from $3.5\text{ }\mu\text{m}$ to $12.6\text{ }\mu\text{m}$ radius. Observed visibilities were slightly smaller than computed visibilities; therefore, some small drops were missed. In Figure 5 of Kumai's article, visibility was plotted versus liquid water content. There was a lot of scatter in the data, and the long-lasting fogs showed far more scatter than the short-period fogs. When visibilities were 1 km or less, the amount of liquid water varied from 0.033 to 0.15 g/m^3 .

Kunkel (1971) used a laser hologram camera to measure drop sizes in fogs. During part of the test, his instrument would only measure large drops. A cascade impactor was used to fill in additional data. During the remainder of the test, droplets with radii as small as $2\text{ }\mu\text{m}$ could be measured. Kunkel's Figure 3 indicated that radii near $45\text{ }\mu\text{m}$ were measured. From his Figure 4, which represented measurements made entirely with one type of instrument, one sees that typical radii were from 5 to $10\text{ }\mu\text{m}$. The number of grams of liquid water varied from 0.021 to 0.148 .

Laktionov et al. (1973) studied statistical characteristics of fog in Russia. They found that the number of droplets with radii less than $8\text{ }\mu\text{m}$ was negatively correlated with the number of droplets with radii greater than $12\text{ }\mu\text{m}$. For example, the number of droplets with radius $18\text{ }\mu\text{m}$ had about a -0.4 correlation with the number of droplets with a radius of $0.45\text{ }\mu\text{m}$. If this should be true in other locations, one would not have to worry that numerous small drops were missed by the measurement technique in fogs with large numbers of large drops. The discussion in Section II of the present report also indicates that small drops contribute much less to extinction than large drops.

Low (1975a) reported on two sets of measurements. The first was done by Dickson at Skelly Field near Ft. Rucker, Alabama. This fog was the radiation type. The wind varied from calm to about 1 m/sec throughout most of its existence. Typical radii were from 9 to $13\text{ }\mu\text{m}$, and maximum radii were about $21\text{ }\mu\text{m}$. Liquid water content at Skelly Field varied from 0.14 to 0.21 g/m^3 .

The second set of measurements reported by Low were in Redwood Valley near Arcata, California. These measurements were made by Bonner and White, but Low has included corrections to errors which were found in their original work. The Redwood Valley fogs were of a mixed radiation-advection type but Low believed that they were predominately radiational. Typical radii were from 4 to $13\text{ }\mu\text{m}$. Information about the maximum radii in the Redwood Valley fogs was not given. The maximum liquid water content was 0.65 g/m^3 and the minimum was 0.04 g/m^3 .

Ludwig et al. (1974) measured droplet size distributions in radiation fog at Brannan Island State Park in the delta of the San Joaquin and Sacramento Rivers. According to their Figures 12 and 24 the largest number of particles were the smallest ones less than a few tenths of a micrometer in radius, and the maximum radius was about $15\text{ }\mu\text{m}$.

Mack et al. (1973) measured fog parameters at sea near Monterey, California, and near the Farallon Islands. Figures 5 and 6 of their report contained many histograms of drop-size distributions. The peaks typically occurred at radii from about 4 to $8\text{ }\mu\text{m}$, and most drop sizes were in the range of 2 - to $16\text{-}\mu\text{m}$ radius. Several distributions were multimodal. The largest radius shown on the graphs was about $31\text{ }\mu\text{m}$. Drizzle occurred during the two most thoroughly studied fogs. It was qualitatively estimated that droplet radii were as large as $100\text{ }\mu\text{m}$. The maximum liquid water content was 0.18 g/m^3 .

May (1961) studied 28 fogs. The method of measurement discriminated against very large and very small droplets. May believed that one could not place an upper limit on the size of a fog droplet because the spectrum merged continuously into that of drizzle or rain when it accompanied a fog. In any case, May's Table 2 indicated a range of droplet radii of 0.25 to 160 μm . In 9 of the 28 fogs the maximum droplet radius was greater than 53 μm and in 11 fogs the maximum radius was less than 28 μm . Other characteristics of the fogs showed a wide variation even though all measurements were taken from the same position on the side of a building on open Salisbury Plain in England. One sample had a minimum radius of 8 μm , and another sample had a maximum radius of 7.5 μm . Three distributions had a median radius less than 0.5 μm but a maximum radius greater than 32 μm . One sample had a median radius of 15 μm . Liquid water contents which were obtained by weighing varied from 0.0044 to 0.27 g/m^3 . Magnitudes computed from the drop-size distributions ranged from 0.0043 to 0.297 g/m^3 .

Mészáros (1965) studied 26 radiation fogs and 13 advection fogs in Budapest, Hungary. Mészáros' Tables I and II listed a great deal of information about each fog, including mode radius, mean radius, mean square radius, mean volume radius, and maximum radius. In the 26 radiation fogs the mode radius varied from less than 0.4 to 10.2 μm , and the mean radius varied from 3.7 to 10.6 μm . Maximum radii in the radiation fogs were in the range from 18.5 to 43.8 μm . Mean liquid water content in the radiation fogs was 0.062 g/m^3 . Average droplets in the 13 advection fogs were larger than the radiation fog droplets. The principal modal radius varied from 2.1 to 12.9 μm . Two advection fogs were bimodal, and in one of these the secondary mode was at 28.0 μm . Mean radii were from 2.2 to 17.0 μm in the advection fogs. Maximum radii in the advection fogs varied from 31.5 to 101.5. In the advection fogs the average liquid water content was only 0.022 g/m^3 , much less than in the radiation fogs.

Okita (1962) examined drops in four radiation fogs in Hokkaido, Japan. Okita made measurements from the surface to 250 m. The largest drops near the surface had radii of 60 μm . Mean radii varied from 6 to 17 μm according to Okita's Figure 20. The maximum liquid water content was about 0.4 g/m^3 near the surface.

Pedersen and Todsén (1960) measured fog droplet sizes near Oslo, Norway. The fogs classified as radiation fogs had maximum radii of about $16\text{ }\mu\text{m}$, and advection fog droplets had radii as large as $25\text{ }\mu\text{m}$. Typical distributions of both kinds of fog were bimodal, and one mode was from 5 to $7\text{ }\mu\text{m}$. In radiation fogs, one mode was typically less than $2\text{ }\mu\text{m}$, and in advection fogs one mode was near $2\text{ }\mu\text{m}$.

Pilié et al. (1975a, b) made extensive micrometeorological measurements in 11 fogs in the Chemung River Valley near Elmira, New York. Measurements were made aloft as well as near the surface. The broadest drop-size distributions always occurred near the surface. Deep fog formed first aloft with its base 30 to 60 m above the surface, but ground fog a few meters thick could result from diffusion of heat to the cold ground. The temperature distribution leading to the formation of a deep valley fog appeared to be the result of nocturnal valley circulations. Further radiative cooling of the fog top produced an unstable lapse rate, and subsequent turbulence caused the fog base to propagate downward to the surface. Typical radii were from 3 to $12\text{ }\mu\text{m}$, and the maximum radius was about $31\text{ }\mu\text{m}$. Most distributions in mature fog at the surface were very broad and multimodal. The average liquid water content at the time of minimum visibility was 0.1 g/m^3 .

Reinking (1975) studied warm radiation fogs under calm conditions in the San Joaquin Valley in California. Maximum radii were about $7.5\text{ }\mu\text{m}$, and typical mean radii were near $3\text{ }\mu\text{m}$. Detailed information was not given.

Roberts (1976) obtained drop-size distributions from Grafenwöhr, Federal Republic of Germany. Roberts' Figure 1, which showed plots of five drop-size distributions, did not indicate that there were any particles with radii greater than $8\text{ }\mu\text{m}$. Most of the distributions had a maximum near the smallest size shown on the curves, about $0.2\text{ }\mu\text{m}$. One of the distributions had a maximum at slightly more than $1\text{ }\mu\text{m}$ and a secondary maximum at about $7.25\text{ }\mu\text{m}$. Roberts' Figure 5 showed that even the small variation in drop-size distributions produced measurable changes in extinction for liquid water contents appropriate to moderate and light fog and mists, although the observations were quite close together for very large liquid water contents and for relatively clear air. For example, for a liquid water content of about 0.007 g/m^3 , extinction of the $10\text{-}\mu\text{m}$ wavelength of energy varied by about a factor of 3, and for about 0.08 g/m^3 extinction varied by a factor of 2. Observations were scarce near 0.03 g/m^3 .

Rogers et al. (1974) investigated the life cycle of California coastal fogs about 1 nmi inland near Vandenberg Air Force Base. The range of radii was typically 1.5 to 115 μm , and the mean radius at a height of 1.2 m was 8.4 μm according to their Table III. Graphical data were not given for 1.2 m but only for heights of 13 m and higher. At the higher levels the distributions tended to peak at about 5- to 7- μm radius. The average liquid water content was 0.08 g/m^3 , and the maximum was 0.12 g/m^3 at the 1.2 m height.

Rozenberg (1974) has summarized expected mean drop sizes for different hydrometeors on page 279 in Table 6.14 of the English translation of the Russian report. The mean droplet radius was 5 μm in thin fogs and 50 μm in medium fogs.

Tag (1976) discussed earlier work which was based on data taken in the Panama Canal Zone. Tag's Figure 2 indicated a maximum radius of about 23 μm . Typical radii would be less than the volume mean radius of 10.8 μm . The liquid water content was 0.39 g/m^3 .

Tampieri and Tomasi (1976a) have fit various drop-size distributions to a modified gamma function. A report describing a study by Vittori and Pesaresi at Baricella in the Po Valley in Italy was among the published work which they discussed. Maximum drop radii were about 22 μm and typical radii were about 8 μm in the fogs in the Po Valley. Tampieri and Tomasi classified these fogs as radiation fogs.

Thompson et al. (1967) have described a laser hologram camera system for measuring drop sizes. Their article contained one sample histogram of data taken at Otis Air Force Base, Massachusetts. Typical radii were near 10 μm , and the maximum radius was about 34 μm .

Thuman and Robinson (1954) studied Alaskan ice-fog particles. The highest temperature at which ice-fog occurred was -30°C during the winter of 1952-1953 at Eielson Air Force Base. Thuman and Robinson were primarily concerned with crystal size as a function of temperature. The minimum size appearing in their Figure 7 was about 13 μm .

Tverskoi (1965) classified fogs as radiation and evaporation fogs in Figure 107, page 324, of the English translation. Two radiation fogs had modal radii between 1 and 2 μm . The graphs showed one radiation fog to have a maximum radius of about 5.5 μm and the other a maximum of 11.5 μm . The modal

radius of the evaporation fog was about $2\text{ }\mu\text{m}$ and the maximum about $10\text{ }\mu\text{m}$. However, Tverskoi stated on a later page that the maximum radii in the fogs were about $60\text{ }\mu\text{m}$.

Webb (1956) gave three representative drop-size distributions in his Figure 4. The radiation fog at Pimmit Green, Virginia, had a modal radius of about $5\text{ }\mu\text{m}$, but the graph was hard to read and the maximum radius was uncertain. Information in the figure caption about the two curves from Washington, D.C., was not consistent with information in Webb's Table 1. One distribution had a modal radius near $7.5\text{ }\mu\text{m}$ and few drops had radii larger than $11\text{ }\mu\text{m}$. The other curve was distinctly bimodal with peaks at 14 and $19\text{ }\mu\text{m}$ radius. This distribution with the large drops was probably the advection fog. It had more drops with radii greater than $20\text{ }\mu\text{m}$ than with radii less than $10\text{ }\mu\text{m}$. The maximum radius was near $70\text{ }\mu\text{m}$. Webb stated that although droplets of $0.3\text{ }\mu\text{m}$ radius could not be seen with certainty, droplets with radii of $0.75\text{ }\mu\text{m}$ were easy to measure by his technique.

In spite of the large amount of work that has been done in measuring fog drop-size distributions, more studies are needed.

It is obvious that in some locations the nature of fog drop-size distributions can change drastically from one time to another. This has been shown very clearly by Grunow (1960), May (1961), and Mészáros (1965). Therefore, the reader is cautioned against assuming that any values in Table 3 are always valid for the specified location. However, there may be places where the life cycle of a fog is almost always similar, but systematic measurements over a period of years will be necessary to demonstrate this.

It should also be noted here that changes in fog characteristics can have very small space and time scales. Richer (1970) found appreciable changes in propagation at 140 GHz ($2142\text{ }\mu\text{m}$) within a fog during a time when no apparent changes in visibility occurred. In Richer's experiment, attenuation increased from 15 to 23 dB/km in a 30-sec period and then decreased to 15 dB/km during the following 30 sec. Zuev et al. (1972) probed a fog with a $0.6943\text{-}\mu\text{m}$ laser. Oscillogram traces of reflected signals showed rapid fluctuations indicating that the inhomogeneities of the fog were in constant motion. George (1972) studied a fog in Washington, D.C., and the length of most elements fell within the range of 50 to 100 ft. Chisholm and Kruse (1974) made mesoscale measurements of visibility at L. G. Hanscom Field in Massachusetts. They found that temporal and spatial variability was much greater in radiation fogs than in advection fogs.

A few investigators have discussed the variation of drop-size distributions during the life cycle of a fog. Pilié et al. (1975b) made one of the most thorough studies of the life cycle of valley fog. They found that shallow ground fog usually occurred before the formation of deep valley fog. The ground fog had mean radii of 2 to 4 μm and a range of 1 to 10 μm . As deep fog formed aloft, mean radii near the surface increased to 6 to 12 μm . Small droplets occurred again at the first visibility minimum after which a bimodal distribution developed at the surface in about half of the fogs. One mode was at a radius of 2 to 3 μm and the other between 6 and 12 μm . Pilié et al. found no consistent change in the shape of drop-size distributions during fog dissipation, but Laktionov (1967b), in a study near Moscow, found that the number of larger drops decreased during fog dissipation. However, Dickson and Hales (1963) have made theoretical computations of visibility changes based upon the assumption that droplets become larger as fog ages. Dickson and Hales did not specifically state that this behavior carried through to the final dissipation stages; their belief was based primarily upon the laboratory part of Findeisen's (1932) study. Low (1975a) examined the life cycles of one radiation fog and four mixed radiation-advection fogs. In the radiation fog, the mean and median radii increased with time from the formative stage to the end of the mature stage and then decreased slightly during dissipation. Behavior was not consistent among the four mixed radiation-advection fogs.

Another characteristic of fogs which has aroused interest is the liquid water content. Many people, including Eldridge (1971) and Barteneva and Polyakova (1965), have suggested that liquid water content should be a simple function of visibility. However, Barteneva and Polyakova's own data in their Figure 2 showed a lot of scatter. Eldridge considered possible observational errors in only two sets of data to conclude that they should be very close together. Koester and Kosowsky (1970) suggested using two relationships: one for radiation fog and one for advection fog. This oversimplification had the merit of illustrating very clearly the pitfall of casually using any equation one might find in the literature. They suggested maximum liquid water contents of 1.0 and 0.4 g/m^3 for radiation and advection fogs, respectively. The earlier part of this section of the present report indicates that most fogs have a liquid water content less than 0.4 g/m^3 . Roberts (1976) measured values slightly more than 1.0 g/m^3 . Low (1975a) reported 0.65 g/m^3 with a visibility of 84 m. In industrial regions of Bohemia in Czechoslovakia Anyz (1964) measured liquid water contents greater than 0.5 g/m^3 with visibilities in excess of 100 m. This could only occur if there were many large drops. Anyz measured 0.606 g/m^3 a short time after the last visibility measurement.

The preceding discussion applies to observations near the surface. Very few observations exist for higher levels, but in one case Okita (1962) observed a liquid water content of 1.6 g/m^3 at a height of 50 m. Rogers et al. (1974) also found that average and maximum liquid water content increased with height, but at 42 m the largest measured liquid water content was only 0.4 g/m^3 . Stalenhoef (1974) found that slant visibility from 40 m was normally less than horizontal visibility at 2 m.

Finally, the reader is urged to remember that a few large drops can make a bigger contribution to extinction than many small drops as has been illustrated in Table 2. This is particularly true at $10.5 \mu\text{m}$, where extinction is comparable to visible extinction for particles with radii greater than $10 \mu\text{m}$. Therefore, the typical radii in Table 3 must not be considered alone without reference to the number of large drops. A maximum radius greater than $30 \mu\text{m}$ was usually an indication of a significant number of large particles.

IV. COMPARISON OF EXTINCTION OF DIFFERENT WAVELENGTHS

Drop-size distributions were taken from six articles. Kumai (1973) and Eldridge (1966) listed data in convenient tabular form. Thirteen of the distributions from Kumai were associated with visibilities less than 1 km and thus came within the definition of fog used in this report. Kumai's fogs typically contained 20 to 40% of radii greater than $10 \mu\text{m}$, and no radii were less than $2.85 \mu\text{m}$. Eldridge's 12 fog drop-size distributions had no radii greater than $8 \mu\text{m}$, and most were less than $1 \mu\text{m}$. Pilié et al. (1975b) and Pedersen and Todsén (1960) provided graphs which were fairly easy to read. Typically, over 10% of radii from Pilié et al. were greater than $10 \mu\text{m}$, but only a few percent from Pedersen and Todsén were greater than $10 \mu\text{m}$. Data were taken from 27 graphs of mature fogs of Pilié et al. and from 3 graphs of Pedersen and Todsén. Garland (1971) and Garland et al. (1973) provided graphs which were difficult to read, but they did provide some supplementary information in tables. Five drop-size distributions were used from each article, and the droplets were typically small. Altogether, extinctions were computed for 65 drop-size distributions.

Figures 3 through 7 illustrate the results of computations made with the 65 drop-size distributions according to the procedure described in Section II.

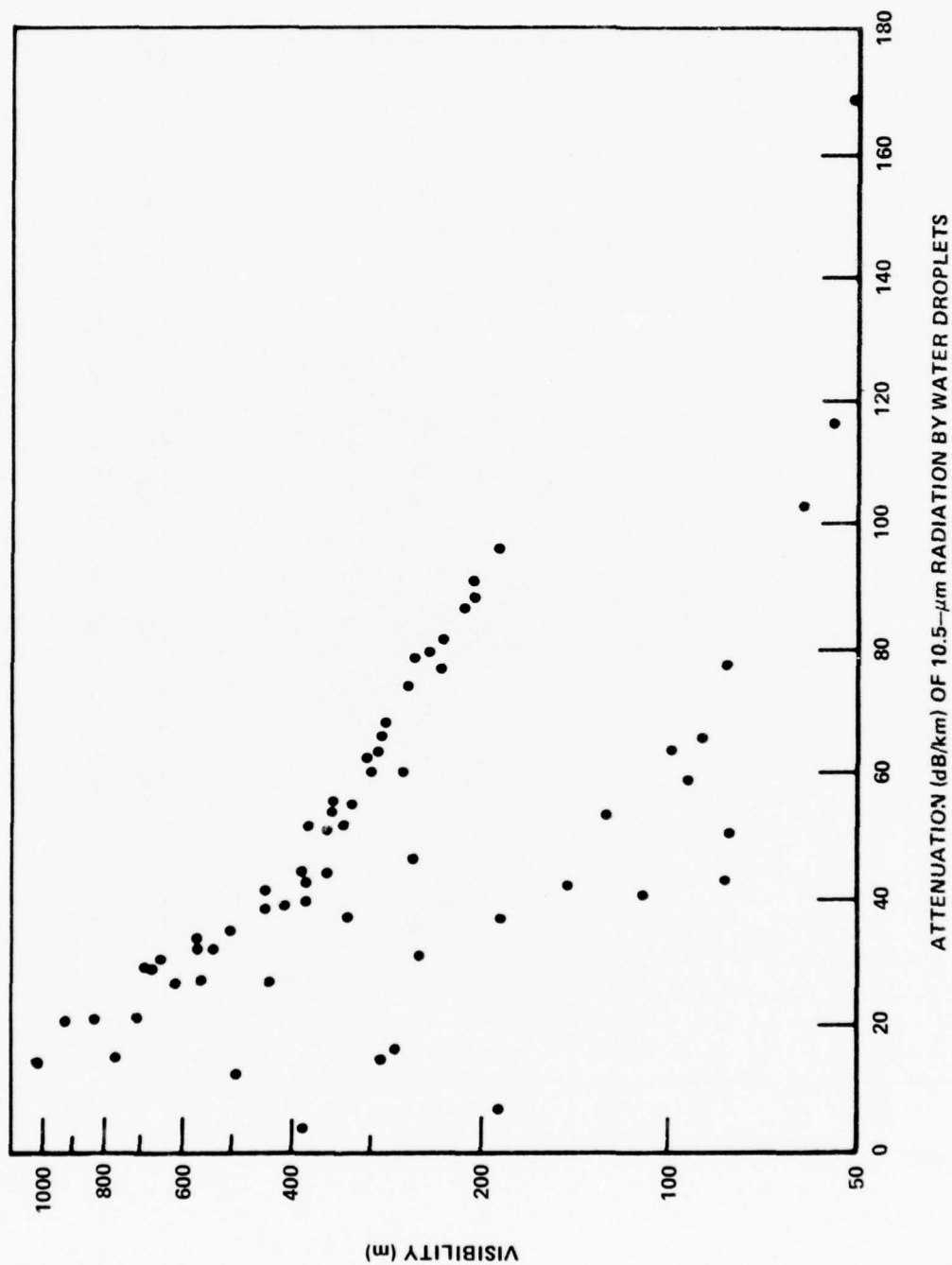


Figure 3. Plot of visibility versus attenuation at 10.5 μm .

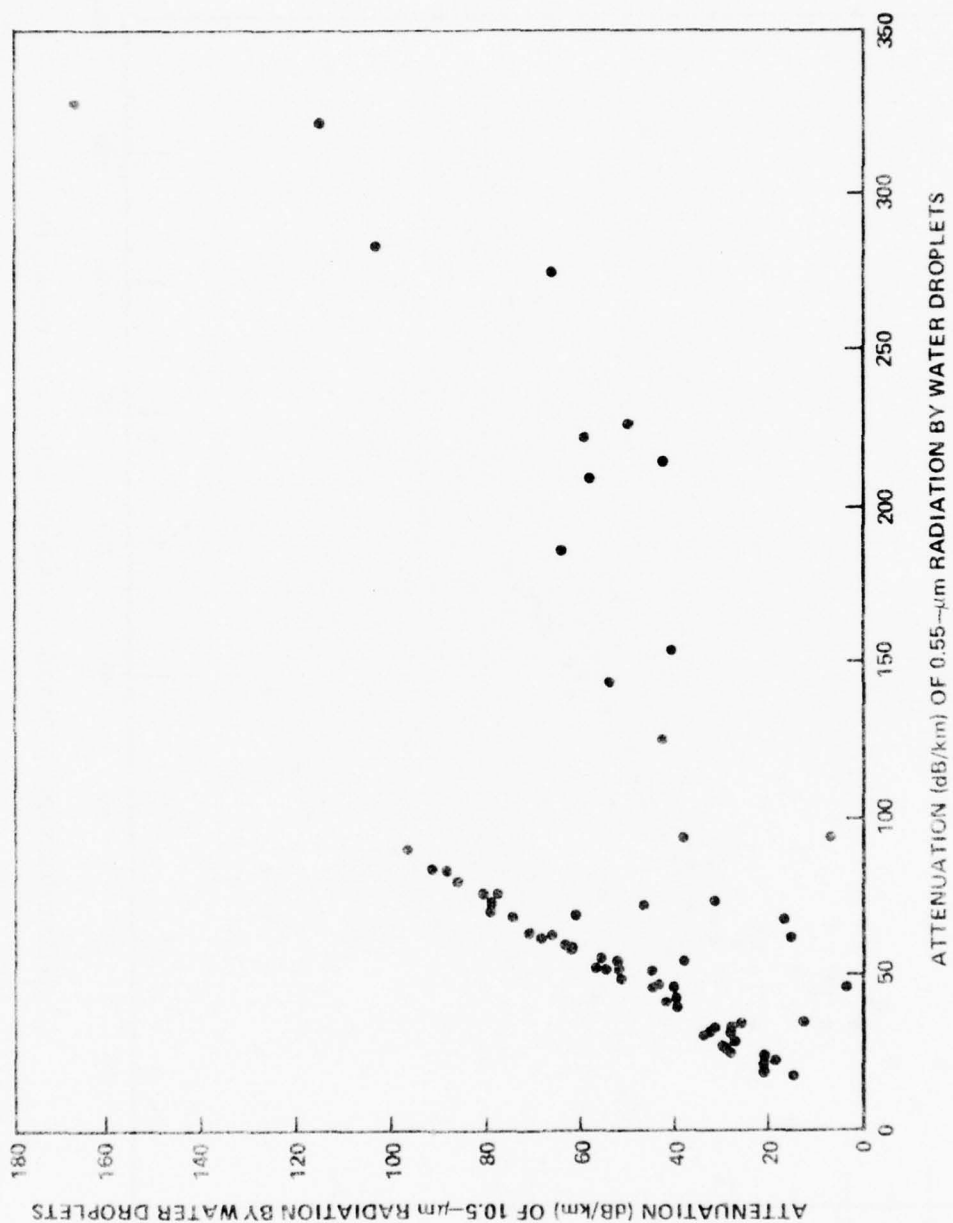


Figure 4. Comparison of attenuation of 10.5- and 0.55-μm radiation by fog droplets.

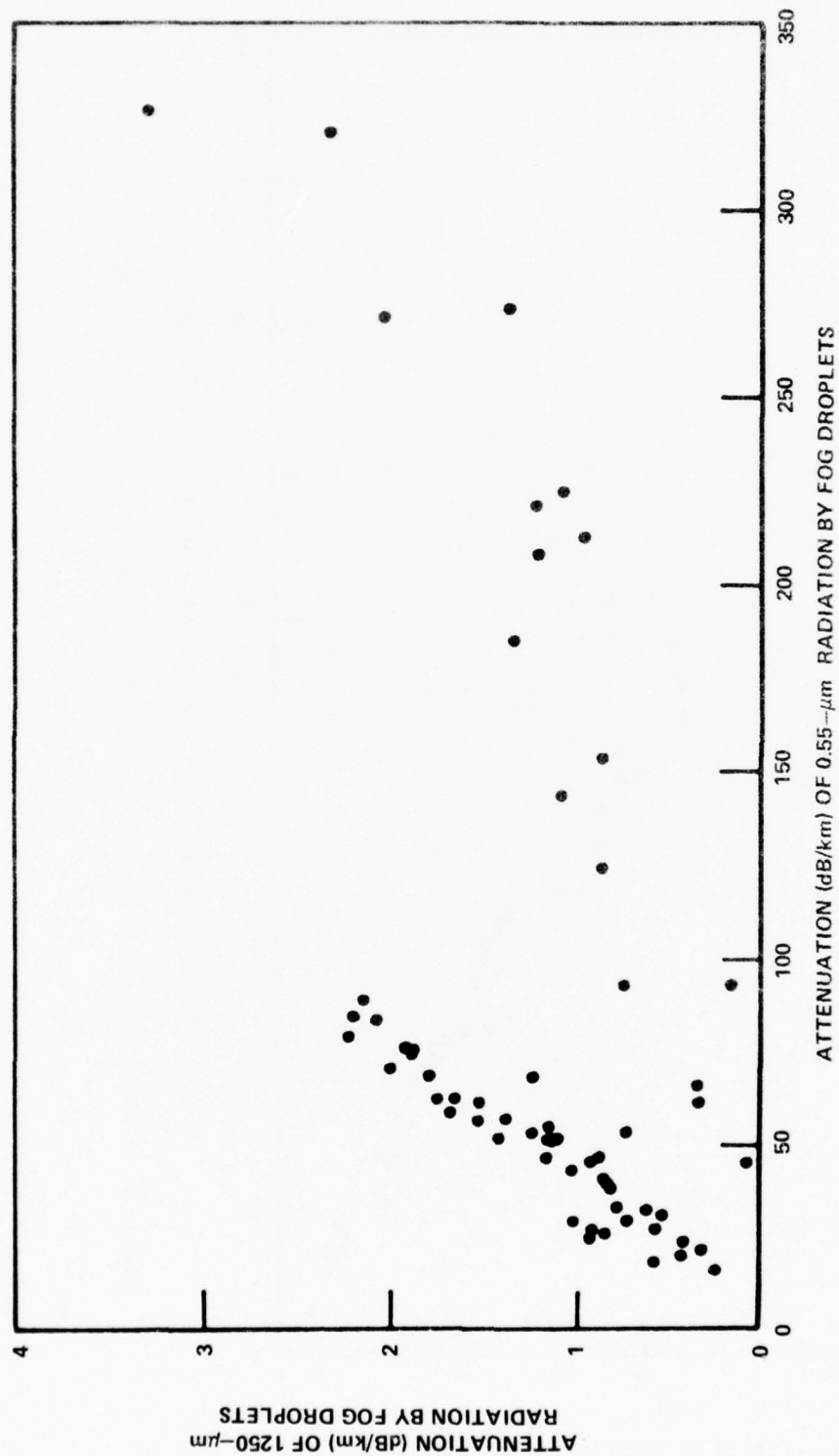


Figure 5. Comparison of attenuation of 1250- and 0.55- μ m radiation by fog droplets.

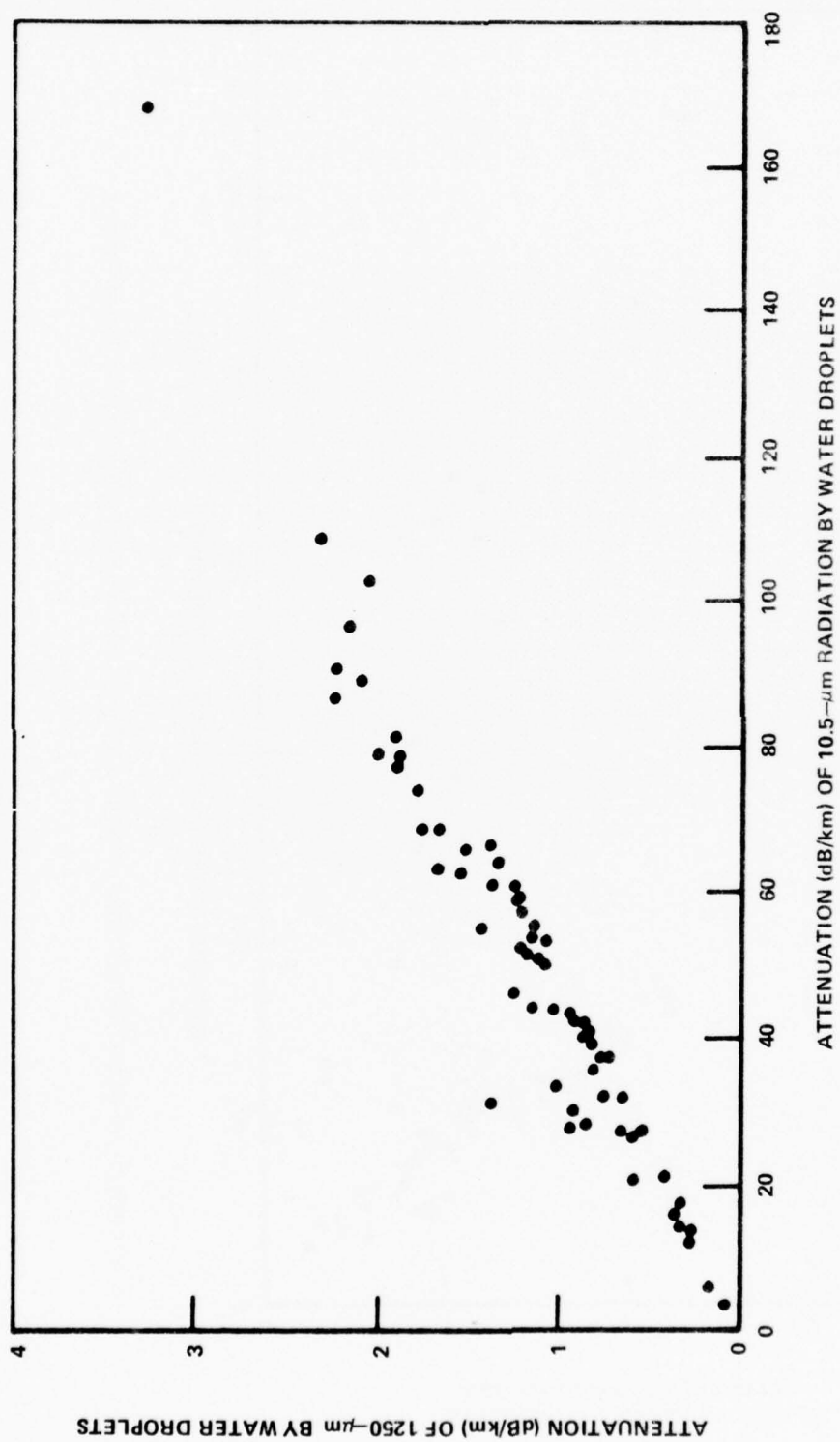


Figure 6. Comparison of attenuation of 1250- and 10.5- μ m radiation by fog droplets.

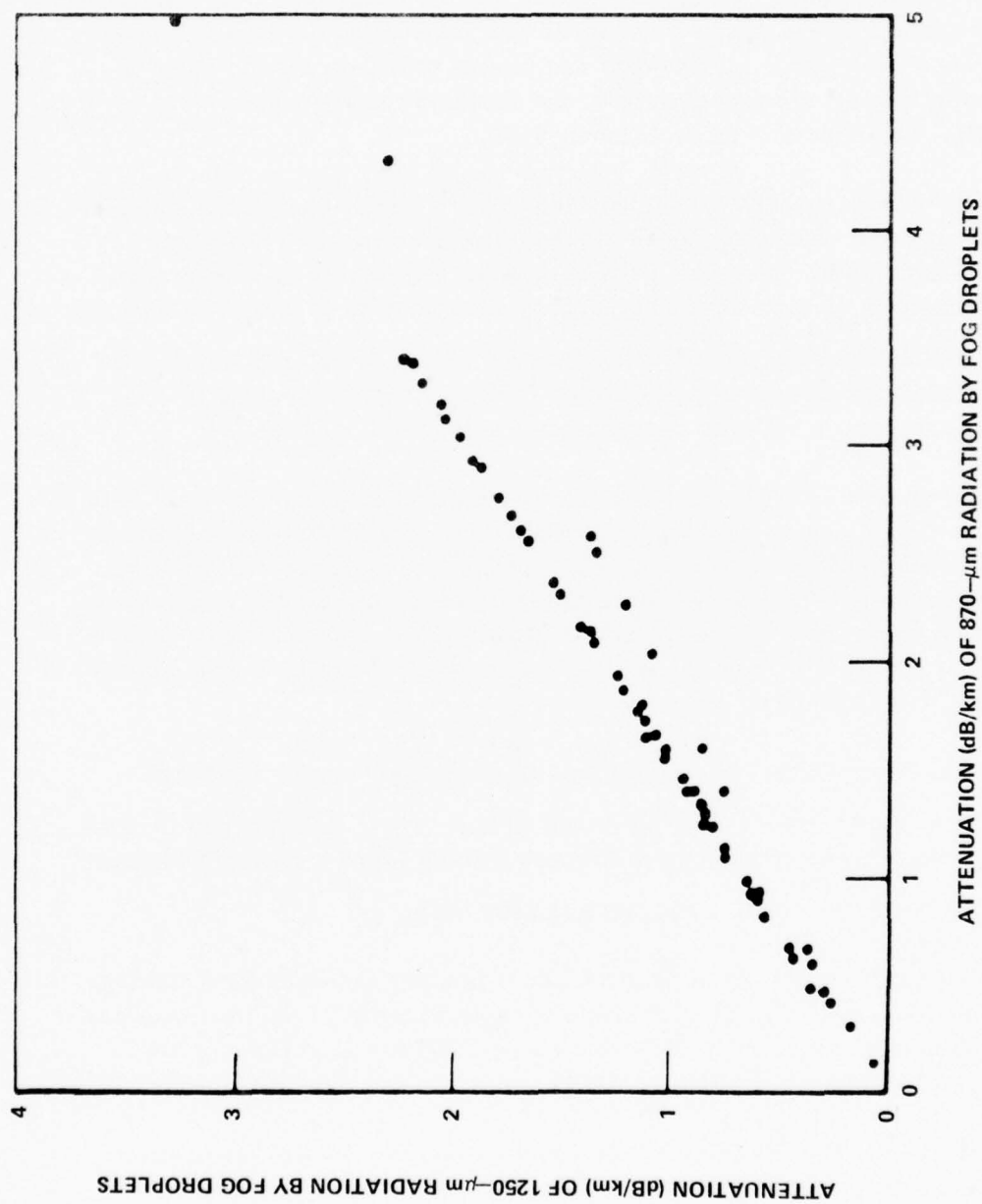


Figure 7. Comparison of attenuation of 1250- and 870- μ m radiation by fog droplets.

Figures 3 and 4 show the relation between attenuations of visible and infrared energy. Figure 3 is a plot of visibility as a function of attenuation at $10.5\ \mu\text{m}$. There is obviously a great deal of scatter in the data. An attenuation of $50\ \text{dB/km}$ at $10.5\ \mu\text{m}$ can be associated with visibilities considerably less than $100\ \text{m}$ or over $300\ \text{m}$. If the data are plotted with both axes in units of decibels per kilometer as in Figure 4, the scatter is still obvious. The correlation of the data in Figure 4 is only 0.61 .

Before comparing these data with the work of others one should consider the following facts. The index of refraction of water does not vary much throughout the visible. Except for the very small drops with radii less than $3\ \mu\text{m}$, the mean Q_{ext} over a reasonable drop-size interval is about the same for different visible wavelengths. The index of refraction of water at $10.5\ \mu\text{m}$ is close to that for wavelengths from 10.0 to $10.6\ \mu\text{m}$, and the parameter $\alpha = 2\pi r/\lambda$ does not vary a lot over this wavelength interval.

Bisyarin et al. (1971) made comparisons of attenuation at $10.6\ \mu\text{m}$ with attenuation at $0.63\ \mu\text{m}$ in real and laboratory fogs. The mean ratio of attenuation at $10.6\ \mu\text{m}$ to attenuation at $0.63\ \mu\text{m}$ was 0.38 for several real fogs and 0.43 for laboratory fogs. It was indicated that about 15% of their ratios were less than 0.20 and about 15% were greater than 0.60 in the real fogs. Sample data in their Figure 5 showed that they were including visibilities greater than $1\ \text{km}$ under their definition of fog.

Chu and Hogg (1968) plotted a graph of wavelength versus expected attenuation by fogs with $0.1\ \text{g/m}^3$ of liquid water. Their estimate for $10.5\ \mu\text{m}$ was $50\ \text{dB/km}$. Some of the fogs in Figures 3 and 4 which attenuated $10.5\ \mu\text{m}$ about $50\ \text{dB/km}$ had a liquid water content near $0.1\ \text{g/m}^3$.

Donati (1973) considered the problem of imaging through hazes and fogs. Calculations indicated that for high visibilities penetration of fog by $10\ \mu\text{m}$ was much greater than penetration by visible energy. Under conditions of low visibility, the infrared offered only modest improvement over the visible.

Johnston and Burch (1967) measured the ratio of $10.0\text{-}\mu\text{m}$ attenuation to $0.546\text{-}\mu\text{m}$ attenuation in artificial fogs in the laboratory. Ratios were measured from 0.54 to 0.79 according to their Table II.

Rensch and Long (1970) used a model of fog drop-size distribution for theoretical computations. It was found that when the radius of drops with the maximum number density was greater than $5\text{ }\mu\text{m}$, the extinction coefficient became wavelength independent for wavelengths from 0.34 to $10.6\text{ }\mu\text{m}$. In my computations, most of the distributions with the radius of maximum number density greater than $5\text{ }\mu\text{m}$ had $0.55\text{-}\mu\text{m}$ and $10.5\text{-}\mu\text{m}$ attenuations within about 10% of each other.

Figure 5 shows the relation of visible and $1250\text{-}\mu\text{m}$ attenuation. These data contain even more scatter than the data in Figure 4. The correlation coefficient for the two attenuations is only 0.49. The correlation between $0.55\text{-}\mu\text{m}$ attenuation and $870\text{-}\mu\text{m}$ attenuation is 0.58.

Figure 6 shows that $10.5\text{-}\mu\text{m}$ attenuation is more closely related to $1250\text{-}\mu\text{m}$ attenuation in fog than it is to $0.55\text{-}\mu\text{m}$ attenuation. The correlation between these two sets of data is 0.9664.

The correlation between $10.5\text{-}\mu\text{m}$ attenuation and $870\text{-}\mu\text{m}$ attenuation is 0.9668 for the 65 fog drop-size distributions used in this study.

Figure 7 contains a plot of $870\text{-}\mu\text{m}$ attenuation versus $1250\text{-}\mu\text{m}$ attenuation. It is obvious that these data are very closely correlated. The correlation coefficient is 0.9873.

Platt (1970) made various approximations and computed an attenuation by fog at $1000\text{ }\mu\text{m}$ of $15.2\text{ dB/km per g/m}^3$.

V. SUMMARY AND CONCLUSIONS

Extinction of electromagnetic energy by fog droplets depends upon the wavelength of the energy, the complex index of refraction of the drops for that wavelength, and the drop-size distribution.

No clear air attenuation is considered in this report. Webster (1973) has provided a good model of atmospheric molecular attenuation. Water vapor will be considered in a future report.

This report considers the following four wavelengths: $0.55\text{ }\mu\text{m}$ in the visible; $10.5\text{ }\mu\text{m}$ in the infrared; $870\text{ }\mu\text{m}$ in the submillimeter range; and $1250\text{ }\mu\text{m}$. Measurements of the complex indices of refraction at these wavelengths for water do not vary much more than about 10% in any study. Variations are much less for the shorter wavelengths. Furthermore, the results of the computations are not influenced much by small changes in the complex index of refraction.

An extensive literature survey shows that the radius of fog droplets can vary from less than $1\text{ }\mu\text{m}$ to more than $100\text{ }\mu\text{m}$. However, a large portion of drops have radii less than $20\text{ }\mu\text{m}$, and few radii are greater than $40\text{ }\mu\text{m}$. In some fogs the maximum radius is as small as $7.5\text{ }\mu\text{m}$, but in other fogs more than half the drops have radii greater than $8\text{ }\mu\text{m}$. These large variations sometimes occur in one location. There may also be large spatial and temporal variations within a fog.

Extinction of energy with a wavelength of $1250\text{ }\mu\text{m}$ is less than extinction of energy with a wavelength of $870\text{ }\mu\text{m}$, regardless of the fog drop-size distribution.

The extinction of these wavelengths near 1 mm by fog droplets is less than the extinction of 0.55 and $10.5\text{ }\mu\text{m}$ in all fogs.

The way the extinction coefficient of $10.5\text{-}\mu\text{m}$ energy compares to the extinction coefficient of $0.55\text{-}\mu\text{m}$ energy depends upon the drop-size distribution. If the maximum drop radius is less than $10\text{ }\mu\text{m}$, extinction of a wavelength of $10.5\text{ }\mu\text{m}$ is less than extinction of a wavelength of $0.55\text{ }\mu\text{m}$. If most of the drop radii are greater than $10\text{ }\mu\text{m}$, the extinction of energy with a wavelength of $10.5\text{ }\mu\text{m}$ is greater than the extinction of energy with a wavelength of $0.55\text{ }\mu\text{m}$. Even a concentration of a fraction of a drop per cubic centimeter with a radius near $30\text{ }\mu\text{m}$ is important because the contribution of a drop to the extinction coefficient depends upon the square of the radius. Computations based upon fog drop-size distributions found in the literature indicate that extinction of the $10.5\text{-}\mu\text{m}$ wavelength is about the same as the extinction of the $0.55\text{-}\mu\text{m}$ wavelength in many fogs.

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